

SUPERLINEAR ELLIPTIC EQUATIONS INVOLVING THE P-LAPLACIAN

PEDRO UBILLA*

This talk is concerned with the existence, nonexistence and multiplicity of solutions for the family of problems

$$\begin{cases} -\Delta_p u = f_\lambda(x, u) & \text{in } \Omega, \\ u > 0 & \text{in } \Omega, \\ u = 0 & \text{on } \partial\Omega, \end{cases} \quad (0.1)$$

where $\Delta_p u := \operatorname{div}(|\nabla u|^{p-2} \nabla u)$ is the usual p-Laplacian, Ω is a bounded domain in \mathbb{R}^N , and $\lambda > 0$ is a real parameter. The initial purpose is to obtain weak solutions of (0.1). Using our hypotheses on f and the regularity theory, these solutions will be in $C^{1,\alpha}(\bar{\Omega})$. A basic feature of the family considered here is its monotone dependence on λ , i.e. $f_\lambda(x, s) \leq f_{\lambda'}(x, s)$ if $\lambda < \lambda'$. The function $f_\lambda(x, s)$ satisfies conditions of local “sublinearity” at 0 and of local “superlinearity” at ∞ mean, roughly speaking, that for x in a subset Ω_1 of Ω , one has

$$\lim_{\substack{s \rightarrow 0 \\ s > 0}} f_\lambda(x, s)/s^{p-1} = +\infty,$$

while for x in another subset Ω_2 of Ω , one has

$$\lim_{s \rightarrow +\infty} f_\lambda(x, s)/s^{p-1} = +\infty.$$

We discuss some works in collaboration with Djairo de Figueiredo and Jean Pierre Gossez as well as one with Humberto Ramos.

*Universidad de Santiago de Chile, Santiago, Chile, pedro.ubillal@gmail.com